

Time : Three Hours]

[Maximum Marks: 300

INSTRUCTIONS

- (i) Answers must be written in English.
- (ii) The number of marks carried by each question is indicated at the end of the question.
- (iii) The answer to each question or part thereof should begin on a fresh page.
- (iv) Your answer should be precise and coherent.
- (v) The part/parts of the same question must be answered together and should not be interposed between answers to other questions.
- (vi) Candidates should attempt **all** the questions.
- (vii) If you encounter any typographical error, please read it as it appears in the text-book.
- (viii) Candidates are in their own interest advised to go through the General Instructions on the back side of the title page of the Answer Script for strict adherence.
- (ix) No continuation sheets shall be provided to any candidate under any circumstances.

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- (2) Frequency
- (3) Velocity
- (4) Wavelength.

OR

- (a) What are group and phase velocities ? Derive the relation between them.
- (b) Give Fresnel's theory of diffraction at straight edge. 20
- (c) Calculate the fringe width of interference pattern produced in Young's double slit experiment with two slits 10⁻³m apart on a screen 1 m away. Wavelength of light used is 5893 Å. 10
- 6. (a) Explain the production and detection of linearly, circularly and elliptically polarised light. 30
 - (b) A diffraction grating used at normal incidence gives a line (5400Å) in certain order superimposed on another line (4050Å) of the next higher order. If the angle of diffraction is 30°, how many lines/cm are there in the grating ?

OR

- (a) Explain the construction and working of Helium-Neon gas laser with energy level diagram.
 20
- (b) Distinguish between Fresnel's and Fraunhoffer diffraction.

2. (a) A frame of reference 's' rotates with respect to another frame of reference 's¹' with an angular velocity \vec{w} . If the position, velocity and acceleration of a particle in frame 's' are represented by \vec{r}, \vec{v} and $\vec{a_0}$. Show that the acceleration of a particle in the frame s¹ is given by

$$\vec{a} = a_0 + 2(\vec{w} \times \vec{v}) + \vec{w}(\vec{w} \times \vec{r}) + \frac{dw}{dt} \times \vec{r}$$
30

- (b) What is a central force ? Give the characteristics of a central force. Show that in a central force field the angular momentum of a particle is conserved.
- (c) An artificial satellite moves in a circular orbit around the earth at a height ½R, from the surface of earth, where R is the radius of the earth. Calculate the period of revolution.

[Given : $R = 6.38 \times 10^6 m$, $g = 9.8 m/s^2$] 10

OR

- (a) Show that $x^2 + y^2 + z^2 c^2 t^2$ is invariant under Lorentz transformation. 15
- (b) Starting from Lorentz transformation equation, for space and time co-ordinates derive equation for relativistic addition of velocities.
- (c) A rocket of mass 20 kg has 180 kg of fuel. The exhaust velocity of fuel is 1.6 kms⁻¹. Calculate the ultimate vertical speed gained by the rocket when the rate of consumption of fuel is 2 kgs⁻¹.

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3. (a) Obtain the expression for work done during adiabatic process.

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- (b) Obtain the expression for Efficiency (η) of a Carnot's engine in terms of temperature of source (T_1) and sink (T_2). 25
- (c) Show that change in entropy during reversible process is zero.

OR

- (a) Derive Maxwell's thermodynamic relations. 20
- (b) Derive the expression for the pressure of an ideal gas on the basis of Kinetic theory of gases. 20
- (c) Find the pressure at which Water would boil at 100°C, if the change specific volume when 1 kg of water is converted into steam is 1.676 m³. 1 atmosphere = 10^{5} Nm⁻² and latent heat of vapourisation of steam = 2.2268×10^{6} JKg⁻¹. 10
- 4. (a) Derive the expression for specific heat of solids on the basis of Einstein theory. 25
 - (b) Discuss Maxwell's law of distribution of velocities for gas molecules.
 - (c) Gold has the same structure of copper. The velocity of sound in gold is 2100 m/s and that in copper is 3800 m/s. If the Debye temperature of gold is 170 K, determine the Debye temperature of copper.

[Given : density of gold = 1.93×10^4 kg/m³; density of copper = 8.96×10^3 kg/m³. Atomic weight of gold =197.0 amu and atomic weight of copper = 63.54 amu.] 10

OR

- (a) Derive Planck's Law of radiation using Einstein 'A' and 'B' coefficients.25
- (b) What is adiabatic demagnetisation ? Deduce thermodynamic expression for cooling produced by adiabatic demagnetization of a paramagnetic salt.
- (c) Calculate the wavelength of the radiation coming out of a furnace at 1500 K that will have maximum intensity. Also specify the type of radiation. Assume Wein's displacement constant to be 2.9×10^{-3} mK.
- 5. (a) Derive the expression for the total energy of particle executing simple harmonic motion. 15
 - (b) What are forced vibrations ? Obtain an expression for displacement in case of forced oscillatory motion. 25
 - (c) A progressive wave travelling along x-axis is given by

 $y = 2 \sin 2\pi (15t - 10x).$

Calculate :

(1) Amplitude

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- (x) Candidates shall put a cross (x) on blank pages of Answer Script.
- (xi) No blank page be left in between answer to various questions.
- (xii) No programmable Calculator is allowed.

(xiii) No stencil (with different markings) is allowed.

- 1. (a) Give the theory of Rutherford α -particle scattering. 20
 - (b) Derive Kepler's First Law of planetary motion on the basis of Newton's law of gravitation. 20
 - (c) A rocket of mass 5000 kg is fired vertically upward from a place at the equator with a velocity of 1200 ms⁻¹. If the angular velocity of the earth is 7.3×10^{-5} rads⁻¹. Calculate the Coriolis force acting on it. 10

OR

(a) Derive the relation $m = \frac{m_o}{\sqrt{1 - \frac{v^2}{c^2}}}$, where the symbols have

their usual meaning.

- (b) Derive Einstein mass energy relation $E = mc^2$. 15
- (c) Water flows through a horizontal pipe of non-uniform cross-section; the pressure is 1 cm of mercury where velocity of flow is 0.35 ms⁻¹. Find the pressure at a point where the velocity is 0.65 ms⁻¹.

(c) When light is incident at an angle of 60° to the normal, the reflected light is plane polarised. What is the refractive index of the transparent refracting medium ? What is the angle of refraction corresponding to the angle of incidence of 60° ? What is the angle between the refracted and reflected components ? 15

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